## Structural Relations

The mathematical properties of phrase structure trees

## Objectives

1. Identify dominance in a tree.
2. Distinguish dominance from immediate dominance.
3. Understand the relationship between exhaustive domination and constituency.
4. Identify precedence in a tree.
5. Understand the constraint against crossing lines.
6. Identify c-command in a tree.
7. Distinguish symmetric from asymmetric c-command.
8. Identify different government relations.
9. Define structurally subject, object, oblique, object of a preposition and indirect object.

## Structural Relations

- Structural relations: the formal relationships between items of a tree
- Why should we care? We want to be able to talk about specific relationships in terms of structures.


## Some basic terms



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Labels: M,N,O,D,E,F,F,G,H,J
Node: Any point with a label

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Terminal nodes

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## Domination

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A dominates $B, C, D, E, F, G$

D dominates E,F,G


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Another way to think of it: "on top of"

## Domination

- A slightly more formal definition:
- Domination: Node A dominates node B if and only if $A$ is higher up in the tree than $B$ and if you can trace a line from $A$ to $B$ going only downwards.


## Immediate Domination

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Node A immediately dominates node B if there is no intervening node $G$ which is dominated by $A$, but dominates $B$. (in other words, A is the first node that dominates B )

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but C immediately dominates only D, E, F

## Exhaustive Domination

- Node A exhaustively dominates a SET of TERMINAL nodes $\{B, C, \ldots, D\}$,
- provided it dominates all the members of the set (so that there is no member of the set that is not dominated by A )
- AND there is no terminal node $G$ dominated by $A$ that is not a member of the set.


## Exhaustive Domination



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## Exhaustive Domination

$$
\begin{aligned}
& \text { A exhaustively dominates the set }\{B, C, D, E\} \\
& \text { A does NOT exhaustively dominate the set }\{B, C, D\} \\
& \text { A does NOT exhaustively dominate the set }\{B, C, D, E, H\}
\end{aligned}
$$

## A formal definition of constituency

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Constituent:The set of nodes exhaustively dominated by a single node

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$\{\mathrm{E}, \mathrm{H}\}$ are NOT a constituent

## Constituent vs Constituent of

- Constituent of does NOT mean the same thing as constituent.
- Essentially 'constituent of' is the opposite of domination.
- $\quad$ dominates $B$, then we say $B$ is a constituent of $A$.
- immediate constituent of is the opposite of immediate domination.


## Some Informal Terms

- Mother: the node that immediately dominates another.
- Daughter: the node that is immediately dominated by another (is an immediate constituent of another).
- Sisters: two nodes that share the same mother.


## Root and Terminal Nodes

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- Root node:A node with no mother


# Root and Terminal Nodes 

- Root node:A node with no mother
- Terminal node:A node with no daughters


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## Precedence

- Precedence: Node $A$ precedes node $B$ if $A$ is to the left of B. (informal definition)
- But this runs into problems with trees which are badly drawn


## Precedence excludes domination

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Is the ball to the left or right of the box?

## Precedence excludes domination

Note that if two nodes are in a domination relation they cannot be in


Is the ball to the left or right of the box? Neither! You can't precede or follow something that dominates (contains) you or you dominate

## Precedence

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- Consider this poorly drawn tree


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## Precedence

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## Does kiss precede clown? Obviously not!

## Precedence

- Consider this poorly drawn tree



## Does kiss precede clown? Obviously not!

What is crucial here is that the dominator of clown precedes the dominator of kissed

## Sister-Precedence

- In order to define precedence we're going to need a more local relation that refers to dominance. This is sister-precedence:
- A sister-precedes $B$ if and only if
- $A$ and $B$ are immediately dominated by the same node
- A appears to the left of $B$


## Precedence

- A Precedes B if and only iff
- A does not dominate $B$ and $B$ does not dominate A AND
- A (or some node dominating $A$ ) sisterprecedes B (or some node dominating B ).


## No Crossing Branches

 Constraint- If one node $X$ precedes another node $Y$ then $X$ and all nodes dominated by $X$ must precede $Y$ and all nodes dominated by $Y$.



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## Sister-Precedence



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NP sister-precedes VP

## Sister-Precedence



NP sister-precedes VP
D sister precedes N

## Sister-Precedence



NP sister-precedes VP
D sister precedes N
N does NOT sister precede V (nor does D)

## Sister-Precedence $\neq$ Immediate Precedence



## Sister-Precedence $=$ Immediate Precedence



N does NOT sister-precede V

## Sister-Precedence $=$ Immediate Precedence



N does NOT sister-precede V
But $N$ does immediately precede $V$

## C-command

- Intuitively: The relationship between a node and its sister, and all the daughters of its sister


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## Note: D does NOT c-command A

## C-command

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- every node dominating $A$ also dominates $B$,
- and $A$ does not itself dominate $B$.


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Sisterhood \&
Aunthood

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- and $A$ does not itself dominate $B$.

you can't command something you dominate


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- SAME THING AS SISTERHOOD


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- A symmetrically c-commands $B$, if $A c-c o m m a n d s$ B AND B c-commands A
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$A \& B$ symmetrically c-command one another


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- A symmetrically c-commands $B$, if $A c-c o m m a n d s ~ B ~ A N D ~$ B c-commands A
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## Asymmetric C-command

A asymmetrically c-commands B , if A c commands B but B does NOT c-command A .

- (intuitively -- A is B 's aunt)


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## Government

- Local version of c-command
- Government (first version): Node A governs node $B$ if $A c$ commands $B$, and there is no node $G$, such that $G$ is $c$-commanded by $A$ and $G$ asymmetrically c-commands $B$.


## Intervenor



## Relativized Government

## Government

Node A governs node B if A c-commands B and there is no node $G$ such that $G$ is $c$-commanded by A and G asymmetrically c-commands B .

Phrase-government: If $A$ is a phrase, then $G$ must also be a phrase.

Head-government: If A is a head (word), G must also be a head.

## Grammatical Relations

- Subject: NP/CP daughter of TP
- Object of a Preposition: NP daughter of PP
- Direct Object:
- With verbs of type $\left.\mathrm{V}_{\left[N P \_N P\right]}, \mathrm{V}_{[N P} \ldots \mathrm{CP}\right]$ and $\mathrm{V}_{[N P}$ _ $N P$ PP] , the NP or CP daughter ofVP
- With verbs of type $\mathrm{V}_{[\mathrm{NP}}$ _ $\left.\mathrm{NP}\{\mathrm{NP} / \mathrm{CP}\}\right\}$, an NP or CP daughter of VP that is preceded by an NP daughter of VP.


## Grammatical Relations

- Indirect Object:This is the Ist object indicating the goal of a verb of transfer (a ditransitive) or the PP of the same kind of verb:
- With verbs of typeV[NP__ NP PP], the PP daughter of VP immediately preceded by an NP daughter of VP.
- With verbs of type V[NP __ NP \{NP/CP\}], the NP daughter of VP immediately preceded by $V$ (i.e. the first NP daughter of VP)
- Oblique: any other NP/PP in the sentence.


## Grammatical Relations

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I gave Adam the book

## Grammatical Relations



I gave Adam the book

## Grammatical Relations



I gave Adam the book

## Grammatical Relations



I gave Adam the book

## Grammatical Relations



I gave Adam the book
I gave the book to Adam

## Grammatical Relations



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## Grammatical Relations



Indirect ObjecĐirect Object Direct Object


I gave Adam the book
I gave the book to Adam

## Grammatical Relations



Indirect ObjecĐirect Object Direct Object


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## Summary

- Structural Relations: relationships between nodes.
- Dominance (=containment)
- immediate dominance (=motherhood)
- exhaustive dominance (=constituent)
- Precedence ( $\sim$ to the left)
- immediate precedence (=adjacent \& to the left)


## Summary

- C-command: sisters \& nieces
- Symmetric C-command: sisters
- Asymmetric C-command:Aunt asymmetrically c-commands nieces
- Grammatical Relations: Subject, Direct Object, Indirect Object, Object of a Preposition.

